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### Abstract

This research dealt with new manner to distinguish among digital photos through Wilks Lambda test. In this way we will know the distinguishing function i.e. its ability to distinguish among digital photos. Then there will be a move to the second stage which represents finding the distinguishing function, which will be used to distinguish among digital photos. After that Mohalanobis scale will be used to know the distance between any communities (i.e. two photos). And in the final stage we will catch the classification mistakes resulted from distinguishing function.

.Wilks Lambda

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( )

: .1

(1921)

"( )

" Karl Pearson's

Tildesley

. [1971 ,Tatsuoka]

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Fisher (1936)

[1971, Tatsuoka]

Smith Brown (1947)

[1971, Tatsuoka]

[Earnshaw, 1994]

[2006, Corl]

(1977 )

( )

[1948, Rao]

(X's)

[1973, Maxwell]

[1951, Bryan]

)

(1977

: .2

: :1.2

:(1) k

$$\left. \begin{array}{l} H_0 : M_1 = M_2 = \dots = M_K \\ H_1 : M_1 \neq M_2 \neq \dots \neq M_K \end{array} \right\} \quad (1)$$

:(2) (Wilks)

$$\Lambda = \frac{|W|}{|T|} = \frac{|W|}{|W - B|} \approx \Lambda(p, n - k, k - 1) \quad (2)$$

W :

B

T

$H_0$

$\Lambda$

$$\Lambda = \frac{|T|}{|W|} \quad (1)$$

(Wilks Lambda) (1)

Source	d.f	SS <sub>p</sub> matrix	Wilks
Between Group	k-1	$B = \sum_{i=1}^k (\bar{X}_j - \bar{X})(\bar{X}_j - \bar{X})'$	$\frac{ W }{ W + B }$
Within Group	n-k	$W = T - B$	
Total	n-1	$T = \sum_{i=1}^k \sum_{j=1}^m (\bar{X}_{ij} - \bar{X})(\bar{X}_{ij} - \bar{X})'$	

$$(3) \quad (1947)$$

(4)

$$\frac{1}{\Lambda} = \frac{|T|}{|W|} = |W^{-1}T| \quad (3)$$

$$= |W^{-1}(W + B)| = |I + W^{-1}B| \quad (4)$$

$$i=1, 2, \dots, r \quad (1 + \lambda_i) \quad W^{-1}B \quad (\lambda_1, \lambda_2, \dots, \lambda_r)$$

$$: (5) \quad \frac{1}{\Lambda} = |I + W^{-1}B|$$

$$\frac{1}{\Lambda} = (1 + \lambda_1) \dots (1 + \lambda_r) \quad (5)$$

(6)

$$V = -[N - 1 - (p + k) / 2] \text{Ln } \Lambda$$

$$= [N - 1 - (p + k) / 2] \text{Ln} (1 + \lambda_1) \dots (1 + \lambda_r) \quad (6)$$

$$= [N - 1 - (p + k) / 2] \sum \text{Ln} (1 + \lambda_i)$$

(2005)  $p(k-1) \chi^2$

$$: (7) \quad V_j \chi^2_{p(k-1)} \quad V$$

$$V_j = [N - 1 - (p + k) / 2] \text{Ln} (1 + \lambda_j) \quad (7)$$

(p+k-2m)

$$p(k-1) \quad (p+k-2)+(p+k-4)+\dots \quad r$$

$$V \quad \dots, V_2, V_1 \quad p = k \quad r = k-1$$

$\chi^2$

$$\left( \frac{V - V_1}{V} \right)$$

:(2)

(2)

Residual After Removing	Approximate $\chi^2$ Statistic	d.f.
First discriminate Function	$V - V_1$	$(p-1)(k-2)$
Second discriminate Function	$V - V_1 - V_2$	$(p-2)(k-3)$
Third discriminate Function	$V - V_1 - V_2 - V_3$	$(p-3)(k-4)$

$\alpha$

$\delta$

p

F

[1959 Raol]

:(8)

F

k

$$F = \frac{ms - 2\lambda I - \Lambda^{1/5}}{p(k-1)\Lambda^{1/5}}$$

(8)

$$df_1 = p(k-1)$$

F

df<sub>1</sub>

$$df_2 = pms - 2\lambda$$

F

df<sub>2</sub>

$$m = N - 1 - \frac{1}{2}(N-P)$$

(9)

$$S = \sqrt{\frac{P^2(1-k)^2 - 4}{(1-k)^2 + P^2 - 5}}$$

(10)

$$\lambda = \sqrt{\frac{P(1-k) - 2}{4}}$$

(11)

(8)

m, S,  $\lambda$

### Mohalanobis Distance

:2.2

[1936 Fisher]

$$Y = a_1 X_1 + a_2 X_2 + \dots + a_p X_p \quad (12)$$

)  $S_y^2$  Y

( $Y_{1q}, Y_{2q}, \dots, Y_{nq}$ ) Y

( t

:(13)

$D^2$

Y

$$D^2 = \frac{(Y + Y)^2}{S_y^2} \quad (13)$$

:2.3

(K > 2)

(i=1,2,3,...,k)                      (n1)                      K

T                      X'=(X<sub>1</sub>, X<sub>2</sub>, ..., X<sub>n</sub>)                      P

:(14)                      n=∑n<sub>i</sub>

$$T = \sum_{i=1}^k \sum_{j=1}^n (X_{ij} - \bar{X})(X_{ij} - \bar{X})' \quad (14)$$

:(15)                      i                      :Wi

$$W_i = \sum_{i=1}^m (X_i - \bar{X})(X_i - \bar{X})' \quad (15)$$

:(16)                      W

$$W = W_1 + W_2 + \dots + W_k \quad (16)$$

:(17)

$$B = T - W \quad (17)$$

$$T = \begin{bmatrix} S_{11T} & \dots & \dots & S_{1pT} \\ S_{21T} & \cdot & \cdot & S_{2pT} \\ \cdot & & & \\ \cdot & & & \\ \cdot & & & \\ S_{p1T} & \dots & \dots & S_{ppT} \end{bmatrix}, \quad W = \begin{bmatrix} S_{11w} & S_{12w} & \dots & S_{1pw} \\ S_{21w} & S_{22w} & \dots & S_{2pw} \\ \cdot & & & \\ \cdot & & & \\ \cdot & & & \\ S_{p1w} & S_{p2w} & \dots & S_{ppw} \end{bmatrix}$$

$$B = \begin{bmatrix} S_{11B} & S_{12B} & \dots & S_{1pB} \\ S_{21B} & S_{22B} & \dots & S_{2pB} \\ \cdot & & & \\ \cdot & & & \\ \cdot & & & \\ S_{p1B} & S_{p2B} & \dots & S_{ppB} \end{bmatrix}$$

( )

$$Y = [Y_1, Y_2, \dots, Y_r]$$

$b \quad \lambda$

(Between Groups)  
(Within Groups)

$$\lambda = \frac{b' B b}{b' W b} \quad (18)$$

$$\frac{\partial \lambda}{\partial b} = \frac{[(b' W b) B b - (b' B b) W b]}{(b' W b)^2} = 0$$

$$(b' W b) B b - (b' B b) W b = 0$$

$\lambda \quad (b' W b)$

$$B b - \lambda W b = 0$$

$$(B - \lambda W) = 0$$

$$(W^{-1} B - \lambda I) b = 0$$

$W^{-1} B$

$\lambda_1$

$\lambda$

.(eigen value)

$$b_1 = (b_{11}, b_{12}, \dots, b_{1p})$$

:(19)

$y_1$

$b_1$

$$y_1 = b_{11} x_1 + b_{12} x_2 + \dots + b_{1p} x_p$$

(19)

$b_2$

$\lambda_2$

$W^{-1} B$

$y_1$

$y_2$

:(20)

$$y_2 = b_{21} x_1 + b_{22} x_2 + \dots + b_{2p} x_p \quad (20)$$

:(21)

$y_2 \quad y_1$

$y_3$

$$y_3 = b_{31} x_1 + b_{32} x_2 + \dots + b_{3p} x_p \quad (21)$$

$y_1, y_2, \dots, y_{r-1}$

$y_r$

( $y_1, y_2, \dots, y_r$ )

:(22)

$$\underline{Y} = \underline{b} \underline{X} \quad (22)$$

$$\underline{Y} = \begin{bmatrix} y_1 \\ y_2 \\ \cdot \\ \cdot \\ y_p \end{bmatrix} = \begin{bmatrix} b_{11} & b_{12} & \cdot & \cdot & b_{1p} \\ b_{21} & b_{22} & \cdot & \cdot & b_{2p} \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ b_{p1} & b_{p2} & \cdot & \cdot & b_{pp} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \cdot \\ \cdot \\ x_p \end{bmatrix}$$



$$B = W^{-1} P W$$

(23)

$$\text{Rank}(W^{-1}B) = \min(k-1, p)$$

(23)

$$R = \min(k-1, p)$$

(24)

.3  
:1.3

(Windows XP)

(Photoshop)  
256

256

Pixels (75\*100)

(75\*100)

(Matlab 7)



1      2      3      4      5      6      7

:(1)

:2.3

:(3)

**Wilks Lambda : (3)**

Wilks Lambda	Statistics	F	df1	df2	Pr
	0.004	12.689	450	3713.1	0

(3)

.( )

:(4)

-241.165	301	-199.302	251	-130.346	201	-145.133	151	-186.99	101	-144.781	51	-135.341	1
-239.94	302	-210.902	252	-124.197	202	-121.613	152	-185.552	102	-137.961	52	-132.39	2
-229.108	303	-209.418	253	-120.352	203	-158.656	153	-182.992	103	-126.114	53	-132.942	3
-222.114	304	-205.87	254	-125.695	204	-173.246	154	-174.25	104	-118.655	54	-131.872	4
-224.451	305	-211.899	255	-131.566	205	-174.967	155	-174.064	105	-103.046	55	-136.193	5
-233.98	306	-213.966	256	-138.979	206	-190.342	156	-183.7	106	-78.743	56	-135.545	6
-237.431	307	-189.031	257	-140.648	207	-170.601	157	-183.387	107	-105.526	57	-139.421	7
-243.404	308	-154.145	258	-141.055	208	-169.743	158	-177.218	108	-110.668	58	-138.64	8
-224.369	309	-173.182	259	-141.154	209	-163.069	159	-187.213	109	-104.913	59	-136.13	9
-223.822	310	-140.668	260	-143.822	210	-155.614	160	-185.477	110	-98.568	60	-137.856	10
-234.814	311	-109.075	261	-138.406	211	-151.562	161	-185.379	111	-112.189	61	-136.064	11
-254.293	312	-158.522	262	-134.631	212	-146.464	162	-187.831	112	-133.408	62	-133.024	12
-257.849	313	-177	263	-134.495	213	-151.676	163	-183.527	113	-139.356	63	-131.196	13
-246.471	314	-128.541	264	-139.173	214	-160.638	164	-173.971	114	-136.327	64	-134.372	14
-242.921	315	-104.141	265	-143.453	215	-165.662	165	-177.016	115	-107.582	65	-136.313	15
-246.501	316	-128.457	266	-144.382	216	-152.75	166	-187.311	116	-113.711	66	-137.912	16
-248.308	317	-181.239	267	-148.474	217	-138.485	167	-182.57	117	-135.38	67	-137.251	17
-251.056	318	-173.309	268	-150.342	218	-134.881	168	-183.361	118	-138.062	68	-137.566	18
-254.707	319	-142.265	269	-151.67	219	-127.356	169	-182.675	119	-122.429	69	-136.476	19
-258.626	320	-117.208	270	-154.332	220	-126.031	170	-178.293	120	-116.429	70	-136.367	20
-253.026	321	-111.279	271	-154.784	221	-127.282	171	-169.495	121	-118.845	71	-136.841	21
-229.71	322	-162.626	272	-153.852	222	-123.905	172	-160.043	122	-136.29	72	-139.565	22
-209.336	323	-176.785	273	-159.721	223	-135.403	173	-153.21	123	-144.139	73	-142.021	23
-208.772	324	-142.628	274	-163.404	224	-142.412	174	-147.214	124	-137.343	74	-142.155	24
-266.289	325	-109.422	275	-160.325	225	-153.719	175	-185.894	125	-133.458	75	-143.758	25
-216.286	326	-71.888	276	-168.086	226	-167.217	176	-186.962	126	-142.821	76	-141.038	26
-225.496	327	-77.462	277	-172.162	227	-180.14	177	-185.974	127	-147.957	77	-144.147	27
-222.407	328	-77.449	278	-175.711	228	-183.942	178	-181.857	128	-140.263	78	-142.668	28
-214.099	329	-65.182	279	-174.175	229	-184.968	179	-183.047	129	-133.823	79	-140.942	29
-232.29	330	-69.088	280	-166.245	230	-184.509	180	-181.533	130	-136.94	80	-153.394	30
-220.274	331	-68.447	281	-158.82	231	-196.341	181	-180.354	131	-128.025	81	-167.403	31
-206.345	332	-61.813	282	-160.482	232	-162.265	182	-181.036	132	-130.797	82	-164.13	32
-226.637	333	-56.815	283	-158.65	233	-133.6	183	-181.812	133	-124.498	83	-144.136	33
-229.06	334	-48.245	284	-156.962	234	-132.56	184	-187.334	134	-116.471	84	-147.066	34
-246.242	335	-51.176	285	-161.699	235	-147.235	185	-196.582	135	-119.115	85	-156.521	35
-266.813	336	-56.437	286	-175.831	236	-164.028	186	-203.253	136	-121.347	86	-157.798	36
-266.63	337	-59.555	287	-190.284	237	-164.21	187	-207.557	137	-116.018	87	-145.045	37
-246.384	338	-59.687	288	-197.06	238	-137.519	188	-212.956	138	-116.18	88	-125.02	38
-224.874	339	-50.354	289	-198.891	239	-153.89	189	-207.57	139	-116.246	89	-123.142	39

-201.474	340	-62.642	290	-202.593	240	-184.484	190	-195.666	140	-114.279	90	-130.332	40
-214.412	341	-66.225	291	-200.101	241	-187.32	191	-176.062	141	-114.759	91	-108.348	41
-246.759	342	-59.174	292	-190.03	242	-172.601	192	-176.557	142	-113.995	92	-123.206	42
-264.213	343	-58.047	293	-185.595	243	-179.091	193	-177.884	143	-111.435	93	-149.568	43
-243.796	344	-58.823	294	-189.849	244	-191.813	194	-183.023	144	-110.296	94	-159.444	44
-195.78	345	-63.84	295	-192.285	245	-185.398	195	-189.98	145	-109.237	95	-159.748	45
-155.28	346	-69.512	296	-193.348	246	-176.252	196	-178.679	146	-108.105	96	-154.16	46
-173.807	347	-59.079	297	-194.592	247	-197.409	197	-168.325	147	-105.63	97	-139.737	47
-187.358	348	-54.638	298	-193.591	248	-193.606	198	-179.641	148	-103.971	98	-128.536	48
-178.096	349	-51.642	299	-190.135	249	-188.064	199	-175.797	149	-102.222	99	-143.97	49
-206.39	350	-51.609	300	-185.113	250	-189.773	200	-169.081	150	-101.012	100	-142.081	50
-201.555	651	-135.976	601	-190.968	551	-103.352	501	-100.105	451	-129.804	401	-247.47	351
-212.589	652	-139.944	602	-206.794	552	-159.375	502	-106.965	452	-128.534	402	-275.611	352
-226.981	653	-127.388	603	-212.011	553	-157.925	503	-98.518	453	-128.319	403	-267.276	353
-210.723	654	-138.5	604	-179.665	554	-172.747	504	-120.778	454	-128.754	404	-228.588	354
-188.676	655	-176.641	605	-140.787	555	-152.106	505	-182.478	455	-129.449	405	-200.086	355
-209.137	656	-199.662	606	-149.689	556	-115.935	506	-117.915	456	-129.156	406	-179.892	356
-189.407	657	-204.6	607	-159.391	557	-138.355	507	-116.061	457	-128.436	407	-248.136	357
-185.189	658	-209.429	608	-154.916	558	-146.803	508	-77.447	458	-127.19	408	-237.371	358
-157.187	659	-216.464	609	-166.662	559	-173.8	509	-70.283	459	-129.066	409	-204.007	359
-157.189	660	-212.663	610	-146.886	560	-164.006	510	-111.789	460	-127.415	410	-223.322	360
-163.123	661	-198.992	611	-142.412	561	-181.7	511	-102.337	461	-127.736	411	-282.451	361
-167.188	662	-190.927	612	-153.422	562	-161.954	512	-102.307	462	-132.597	412	-288.383	362
-173.498	663	-195.649	613	-147.315	563	-136.579	513	-145.732	463	-139.004	413	-242.629	363
-177.793	664	-188.598	614	-150.304	564	-155.338	514	-123.659	464	-146.907	414	-203.249	364
-151.296	665	-183.034	615	-158.153	565	-176.767	515	-87.276	465	-148.267	415	-158.515	365
-144.584	666	-197.356	616	-161.642	566	-155.106	516	-133.907	466	-145.305	416	-243.735	366
-131.368	667	-223.591	617	-161.931	567	-199.302	517	-116.103	467	-130.053	417	-285.428	367
-124.877	668	-208.67	618	-172.651	568	-197.8	518	-88.991	468	-142.609	418	-221.494	368
-126.125	669	-200.4	619	-186.992	569	-177.662	519	-92.456	469	-150.87	419	-182.388	369
-140.072	670	-215.178	620	-169.322	570	-139.015	520	-125.174	470	-146.384	420	-213.494	370
-108.212	671	-221.717	621	-155.226	571	-132.948	521	-112.836	471	-137.555	421	-233.593	371
-90.325	672	-205.789	622	-159.511	572	-180.736	522	-82.999	472	-132.826	422	-237.482	372
-169.589	673	-217.857	623	-195.881	573	-199.639	523	-86.283	473	-130.974	423	-265.079	373
-250.475	674	-257.077	624	-178.665	574	-161.057	524	-91.672	474	-127.298	424	-236.671	374
-196.851	675	-189.045	625	-185.817	575	-200.191	525	-95.626	475	-123.402	425	-207.767	375
-151.589	676	-218.21	626	-196.141	576	-192.849	526	-88.78	476	-123.821	426	-183.38	376
-180.366	677	-229.169	627	-190.318	577	-188.29	527	-81.409	477	-124.608	427	-210.578	377
-204.348	678	-224.546	628	-189.784	578	-191.315	528	-80.971	478	-124.866	428	-246.515	378
-199.059	679	-229.454	629	-216.251	579	-188.355	529	-93.729	479	-113.826	429	-228.087	379
-204.029	680	-229.069	630	-233.21	580	-181.17	530	-106.537	480	-102.07	430	-210.569	380
-220.075	681	-221.407	631	-209.37	581	-162.969	531	-78.743	481	-100.538	431	-193.873	381
-217.466	682	-219.632	632	-203.993	582	-182.179	532	-95.665	482	-100.386	432	-218.039	382
-218.009	683	-259.169	633	-194.155	583	-155.284	533	-103.57	483	-72.568	433	-226.633	383
-215.107	684	-246.137	634	-187.773	584	-127.431	534	-98.967	484	-82.61	434	-193.147	384
-197.231	685	-215.918	635	-217.448	585	-132.225	535	-83.922	485	-89.428	435	-184.484	385
-200.307	686	-186.314	636	-187.557	586	-158.288	536	-82.523	486	-84.869	436	-213.933	386
-198.048	687	-185.237	637	-172.932	587	-152.327	537	-97.415	487	-78.932	437	-228.983	387
-224.482	688	-203.548	638	-193.122	588	-148.353	538	-112.728	488	-83.792	438	-247.971	388
-190.545	689	-219.258	639	-177.937	589	-152.309	539	-100.73	489	-89.685	439	-237.373	389
-198.849	690	-225.912	640	-191.907	590	-143.745	540	-94.525	490	-90.145	440	-208.901	390

-196.941	691	-219.753	641	-213.151	591	-166.665	541	-85.049	491	-70.617	441	-179.736	391
-206.336	692	-221.438	642	-242.251	592	-174.189	542	-77.572	492	-57.696	442	-163.657	392
-177.095	693	-229.467	643	-202.571	593	-175.188	543	-80.798	493	-51.849	443	-169.051	393
-178.914	694	-229.542	644	-194.256	594	-166.914	544	-89.937	494	-60.322	444	-181.069	394
-177.59	695	-219.017	645	-220.583	595	-153.014	545	-93.386	495	-79.682	445	-194.601	395
-175.332	696	-208.703	646	-171.285	596	-158.358	546	-86.858	496	-90.687	446	-206.807	396
-180.097	697	-206.937	647	-169.147	597	-155.817	547	-99.134	497	-91.652	447	-165.483	397
-214.235	698	-211.015	648	-202.517	598	-164.078	548	-102.693	498	-89.78	448	-165.384	398
-218.962	699	-195.573	649	-181.189	599	-127.195	549	-105.522	499	-76.889	449	-158.889	399
-237.667	700	-194.301	650	-157.916	600	-163.836	550	-105.981	500	-124.529	450	-145.642	400

:(5)

Mahalanobis Distance							
	Five	Four	ONE	TWO	seven	six	three
Five	0.00000	47.91119	13.49562	32.06681	25.13006	29.70336	13.09592
Four		0.00000	36.08924	53.41932	27.61353	29.06947	43.55979
ONE			0.00000	30.34995	12.59903	12.90983	5.70007
TWO				0.00000	28.09035	34.72476	31.46415
seven					0.00000	10.57803	14.21088
six						0.00000	17.83970
three							0.00000

(5)

:(6)

Plug-in classification table							
	Five	Four	ONE	TWO	seven	six	three
Five	84	0	16	0	0	0	0
Four	0	96	0	0	2	2	0
ONE	0	0	99	0	0	0	1
TWO	0	0	0	97	2	0	1
seven	0	1	6	1	84	4	4
six	0	1	7	0	8	84	0
three	0	0	23	3	4	0	70

(6)

(2)

16

84

96

99

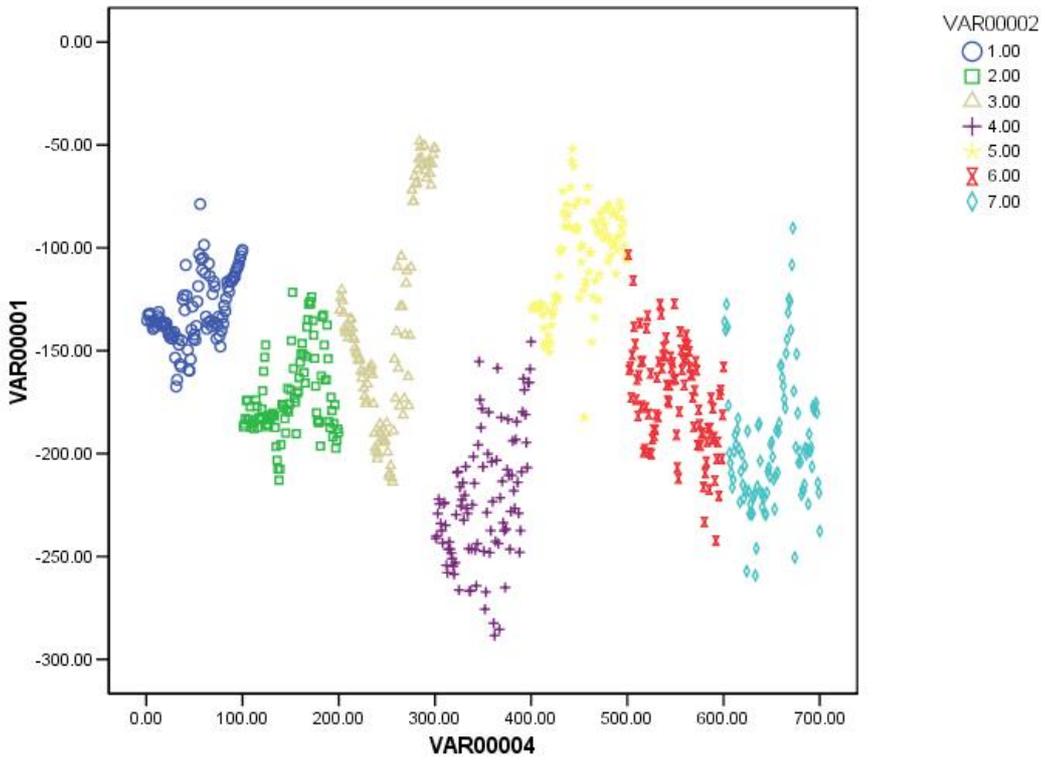
97

84

84

23

70



( )

:(2)

: :3.3

( )

(1

.(Wilk's Lambda)

( )

(2

( )

( )

(700)

(3

(2)

( )



(4)

(2)

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(1)

(2000)

(2)

(2005)

(3)

(1977)

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